

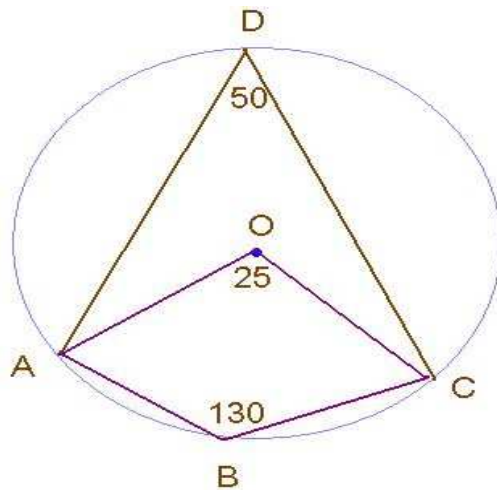
Second Terminal Examination 2012

Maths

Class : 10

1) The difference between any two terms of an arithmetic sequence is a multiple of it's common difference . Since 100 is not a multiple of 7 the difference between any two terms of the given sequence can not be 100

2)



It given as $\angle ABC = 130^\circ$.

In cyclic quadrilateral ABCD , $\angle D = 50^\circ$ (Opposite angles of a cyclic quadrilateral)

Hence $\angle AOC = 50 \times 2 = 100^\circ$ (By theorem)

3) Remainder obtained on dividing $p(x)$ by $(x-2)$ is $p(2)$

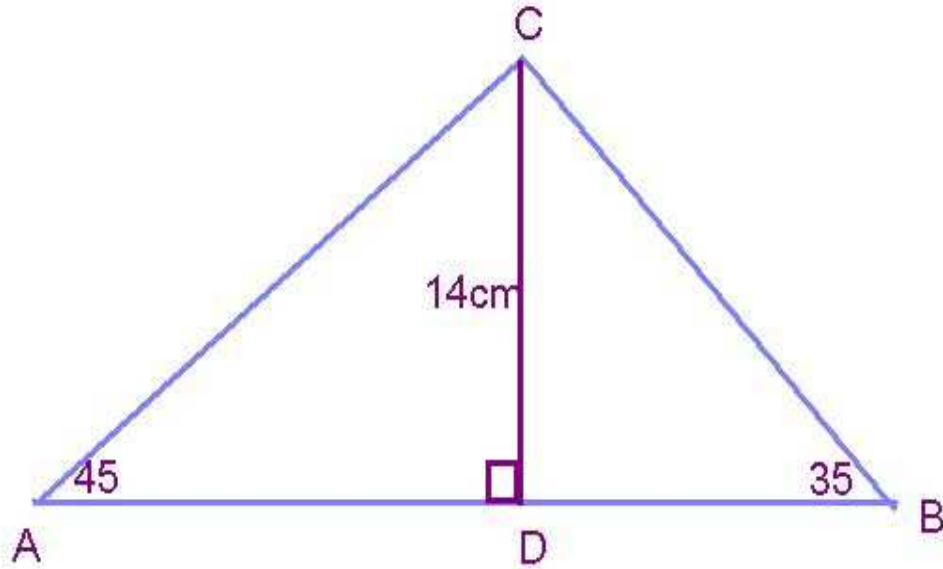
$$P(2) = 2(2)^3 - 3(2)^2 + 5(2) - 10$$

$$= 16 - 12 + 10 - 10 = 4$$

The remainder is 4

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4)



In $\triangle ACD$ angles are 45,45,90 hence sides are in the ratio $1 : 1 : \sqrt{2}$. Since $CD=14\text{cm}$ we have $AD=14\text{cm}$.

From $\triangle BCD$

$$\tan 35 = \frac{CD}{DB}$$

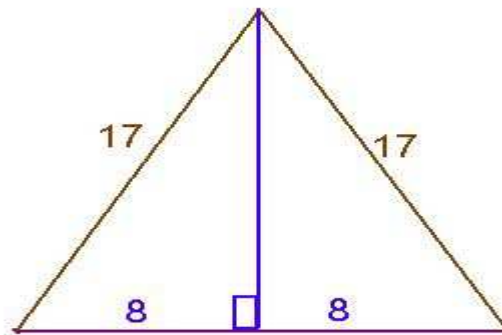
$$0.70 = \frac{14}{DB}$$

$$DB = \frac{14}{0.7} = 20$$

Therefore $AB = AD+DB = 14+20 = 34 \text{ cm}$

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5)



$$l^2 = 17^2 - 8^2$$

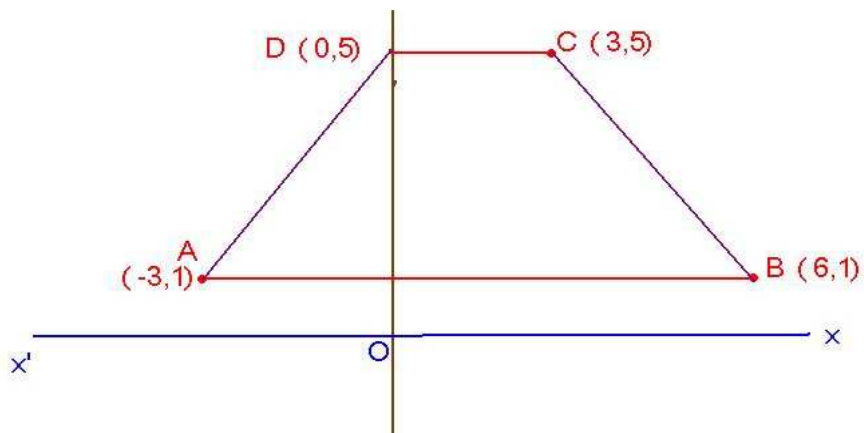
$$l^2 = 289 - 64 = 225$$

$$l = \sqrt{225} = 15\text{cm}$$

Slant Height = 17cm

$$\text{L.S.A} = 2bl = 2 \times 16 \times 15 = 480\text{cm}^2$$

6)



ABCD is an isocles trapezium

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7)

a) Probability of getting a black bead = $\frac{6}{18} = \frac{1}{3}$

b) Probability of getting a black bead in 2nd case = $\frac{7}{20}$

Probability of getting a black bead in the 1st case = $\frac{6}{18} = \frac{1}{3}$

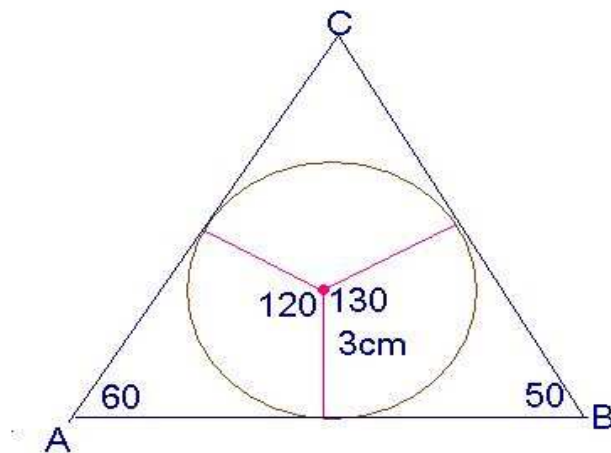
$\frac{7}{20} > \frac{1}{3}$ hence probability of getting a black bead increases in the 2nd case

Probability of getting a white bead in 2nd case = $\frac{13}{20}$

Probability of getting a black bead in the 1st case = $\frac{12}{18} = \frac{2}{3}$

$\frac{13}{20} < \frac{2}{3}$ hence probability of getting a white bead decreases in the 2nd case

8)



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9)

a) Sum of angles in each polygon = $(9-2)180 = 7 \times 180 = 1260^\circ$

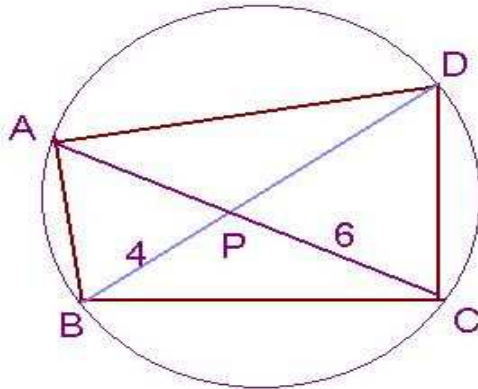
b) $n \times \text{midterm} = \text{sum}$

$9 \times 5^{\text{th}} \text{ term} = 1260$

$5^{\text{th}} \text{ term} = 1260/9 = 140$

Measure of each angle noticed by Dhanya is 140°

10)



Given as BD bisects AC also $PC=6\text{cm}$ hence $PA=6\text{cm}$

$$PA \times PC = PC \times PA$$

$$6 \times 6 = 4 \times PD$$

$$PD = 36/4 = 9\text{cm}$$

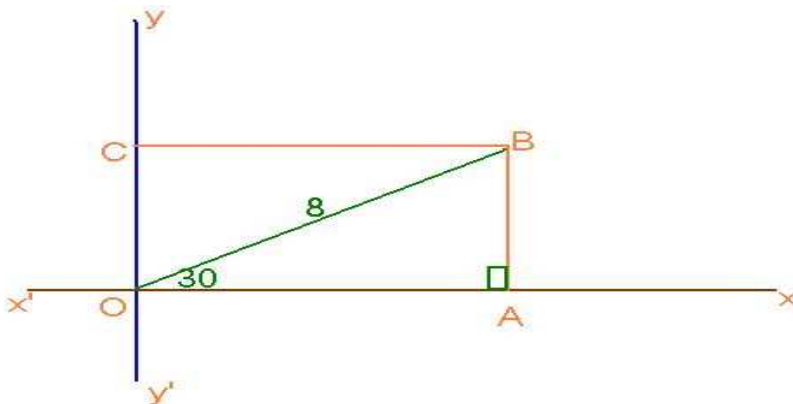
Hence $AC = 12\text{cm}$ and $BD=13\text{cm}$

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11) a) Probability of getting a perfect square in both slips = $\frac{24}{1250}$

b) Probability of getting multiples of 5 in both paper slips = $\frac{50}{1250}$

12)



In ΔOAB angles are $30^\circ, 60^\circ, 90^\circ$ hence sides are in the ratio $1 : \sqrt{3} : 2$.

Since $OB=8$ units we have $AB=4$ units and $OA=4\sqrt{3}$ units.

Co ordinate of the point A is $(4\sqrt{3}, 0)$

Co ordinate of the point B is $(4\sqrt{3}, 4)$

Co ordinate of the point C is $(0, 4)$

13)

Number of rows = x

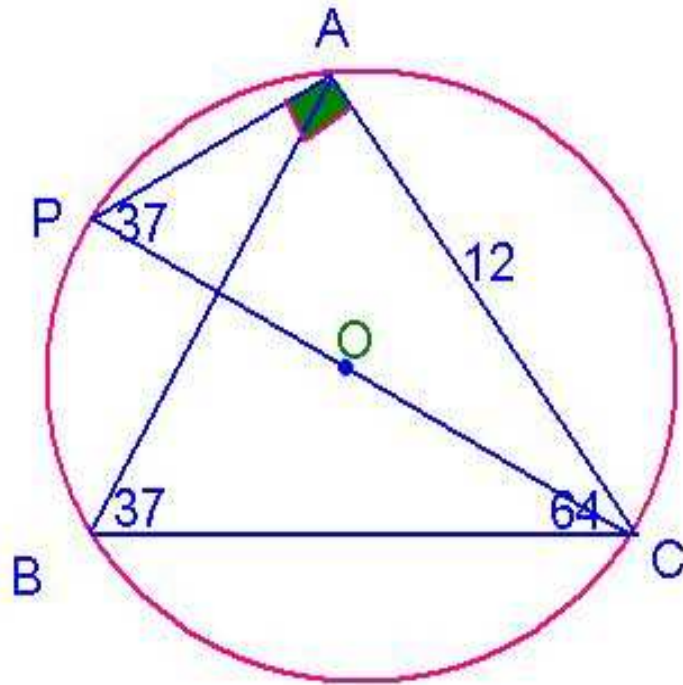
Number of columns = $3x+1$

$$x(3x+1)=200, 3x^2+x-200=0$$

Solving we get $x=8$

Hence number of rows = 8 and number of columns = 25

14)



$\angle P = 37^\circ$ (Angles in same segment)

$\angle PAC = 90^\circ$ (Angle in a semicircle)

From ΔPAC

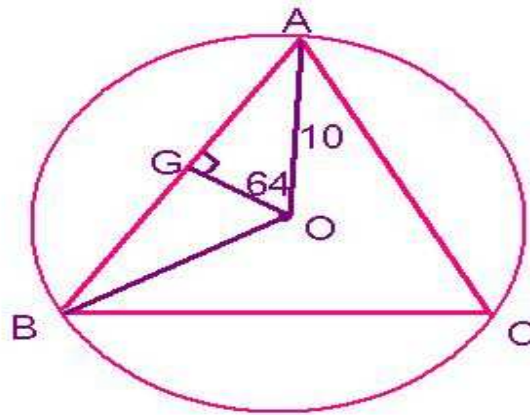
$$\sin 37 = \frac{12}{PC}$$

$$0.60 = \frac{12}{PC}$$

$$PC = \frac{12}{0.6} = 20\text{cm}$$

Circum radius = 10cm

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From ΔAOG

$$\sin 64 = \frac{AG}{10} \quad 0.90 = \frac{AG}{10}$$

$$AG = 0.90 \times 10 = 9\text{cm}$$

$$AB = 2 \times 9 = 18\text{cm}$$

15)

$$\frac{x}{360} = \frac{r}{R}$$

$$\frac{288}{360} = \frac{r}{15}$$

$$r = 12\text{cm} . \text{ Radius of the cone} = 12\text{cm}$$

$$\text{Volume of the cone} = \frac{1}{3} \times \pi \times 12 \times 12 \times 9$$

$$= 1356.48\text{cm}^3$$

$$\text{Volume in liters} = 1356.48/1000 = 1.356 > 1.5$$

Hence the vessel is not sufficient to buy 1.5 liters coconut oil

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16)

$\angle ADB = 50^\circ$ (Each angle between a chord and the tangent at one of its ends in a circle is equal to the angle in the segment on the other side of the chord ,

$\angle CBD = 40^\circ$ (")

$\angle BDC = 20^\circ$

$\angle BCD = 120^\circ$ (angles in a triangle)

17)

a) $3(2)^3 - 13(2)^2 + k(2) + 12 = 0$

$$24 - 52 + 2k + 12 = 0$$

$$2k = 52 - 36 = 16$$

$$k = 8$$

$$p(x) = 3x^3 - 13x^2 + 8x + 12$$

b) remainder obtained on dividing $p(x)$ by $(x-1)$ is $p(1)$

$$p(1) = 3 - 13 + 8 + 12 = 10$$

Remainder is 10

c) -10 is to be added to become $(x-1)$ a factor

Or

$$P(x) = 6x^2 - x - 2$$

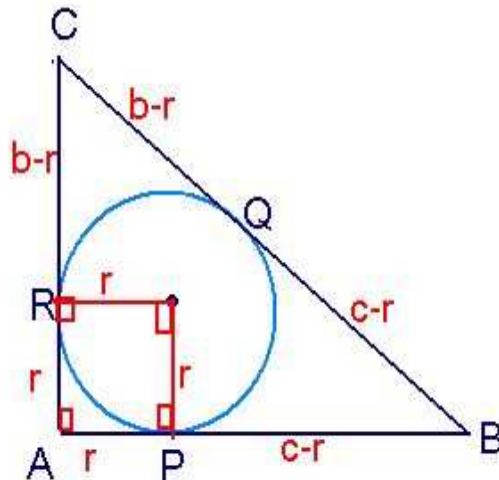
$$P(x) = 0$$

$$6x^2 - x - 2 = 0 \text{ solving we get } x = 2/3 \text{ and } x = -1/2$$

If $p(2/3) = 0$ $(3x-2)$ is a factor If $p(-1/2) = 0$ $(2x+1)$ is a factor

Hence the first degree factors are $(3x-2)$ and $(2x+1)$

18)



Let $AB=c$, $AC=b$ and $BC=a$. O be the incentre of ΔABC and r be the inradius
 $\angle ORA = 90^\circ$ (radius and tangent) in the same way $\angle OPA = 90^\circ$. $\angle A = 90^\circ$ (given)
Hence $\angle POR = 90^\circ$ (angles in a quadrilateral). Therefore $OPAR$ is a square of sides r .

$AP=AR=r$ (tangents from external points)

In the same way $BP=BR =c-r$, $CQ=CR =b-r$

$$b-r+c-r = a$$

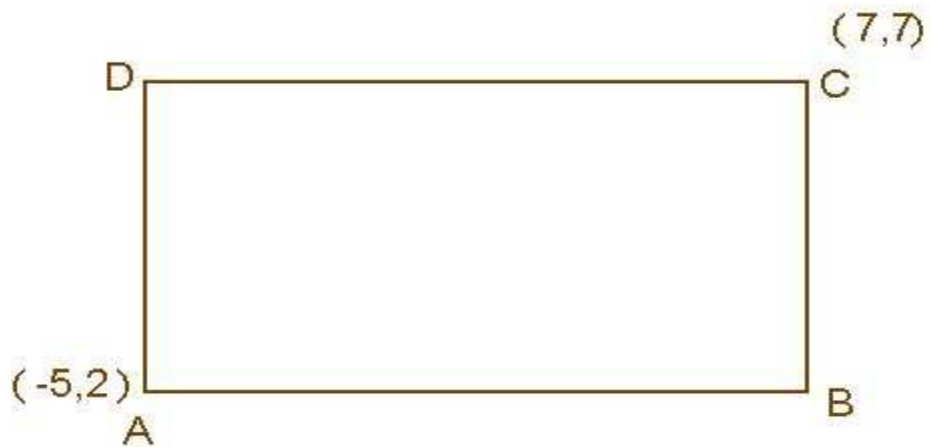
$$b+c-a = 2r$$

$$AC+AB-AC = 2r$$

Hence the proof

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19)

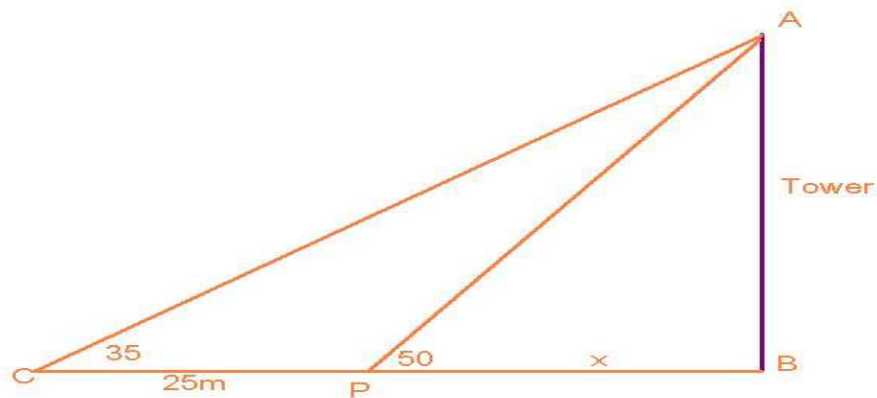


- a) Coordinates of other vertices are $B(7,2)$ and $D(-5,7)$
- b) $AB=12$ units and $AD=5$ units
- c) Length of diagonal = 13 units

20) Construct incircle and measure the inradius

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21)



In the figure AB represents height of the tower and P,C represents the position of boy. Let $PB=x$

From ΔABP

$$\tan 50 = \frac{AB}{x}, \quad 1.20 = \frac{AB}{x}$$

$$AB = 1.20x \text{-----(1)}$$

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From ΔABC

$$\tan 35 = \frac{AB}{BC} \qquad 0.7 = \frac{1.20x}{x+25}$$

$$0.7x + 17.5 = 1.2x$$

$$0.5x = 17.5$$

$$x = 17.5/0.5 = 35$$

$$\text{Height of tower} = 1.2 \times 35 = 42\text{m}$$

$$22) \quad \frac{1}{3} \pi r^2 h = 320\pi$$

$$5r^2 = 320$$

$$r^2 = 64$$

$$r = 8\text{cm}$$

$$\text{T.S.A} = \pi \times 8 \times 17 + \pi \times 8 \times 8 = 200\pi \text{ cm}^2$$

23) There is a small mistake in the question. It is not square prism it is square pyramid

Let sides of the cube be 'a'

Square pyramid

Base edge = 'a' and height = a then volume = $\frac{1}{3}a^3$

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Cone

$$\text{Radius} = \frac{1}{2} a \text{ and height} = a \text{ then volume} = \frac{1}{3} \pi r^2 h = \frac{1}{3} \pi \left(\frac{a}{2}\right)^2 a = \frac{1}{3} \pi \frac{a^3}{4} = \frac{1}{12} \pi a^3$$

Sphere

$$\text{Radius} = \frac{1}{2} a \text{ then volume} = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi \left(\frac{a}{2}\right)^3 = \frac{4}{3} \pi \frac{a^3}{8} = \frac{1}{6} \pi a^3$$

$$\text{Ratio of volumes} = \frac{1}{12} \pi a^3 : \frac{1}{6} \pi a^3 = \frac{1}{12} : \frac{1}{6} = \frac{1}{12} \times \frac{12}{1} : \frac{1}{6} \times \frac{12}{1} = 1 : 2$$